

## Examen parcial de Sistemes Gràfics Interactius (SGI)

Curs 2012-13, 16 d'abril 2013

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Name :

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**Question 1.** Explain what an *ambiguous* 3D model is. Give an example of a representation scheme that might be ambiguous for representing solid models.

**Question 2.** Let  $A, B$  be two surfaces. We know that there exists a homeomorphism between  $A$  and  $B$ . What can we state about  $A$  and  $B$ ?

**Question 3.** For some pointset  $S$  we know that  $S = \text{cl}(\text{Int}(S))$ , that is,  $S$  equals the closure of its interior. What can we say about the topology of  $S$ ?

**Question 4.** Compute the genus of a solid object bounded by a single shell with 10 faces, 24 edges, 16 vertices and 2 rings.

**Question 5.** We want to write an efficient Python algorithm for counting the number of concave edges in a Blender mesh.

(a) Describe briefly the major steps of the algorithm. Indicate clearly which incidence relationship you need to build.

(b) Give the (average case) time complexity of the algorithm.

**Question 6.** A single piece of Emmental-like cheese such as the one on the figure has (select the correct choice):



- (a) Single cell, many shells, large genus
- (b) Many cells, single shell, large genus
- (c) Many cells, single shell, small genus
- (d) Single cell, many shells, small genus

**Question 7.** Which Boolean operation(s) will you choose to model a solid similar to the cheese object above using CSG?

**Question 8.** Explain how "face" vertices are computed in the Catmull-Clark subdivision scheme. Does the computation of "face" vertices require any additional topological relationship beyond those provided by Blender?

**Question 9.** For a valid polyhedron, indicate the cardinality of the following topological relationships:

- (a)  $E:\{F\}$
- (b)  $E:\{V\}$

**Question 10.** Indicate the minimum cardinality for the following topological relationships, assuming a valid BRep:

- (a)  $V:\{E\}$
- (b)  $V:\{F\}$

**Question 11.** Building efficiently the  $V:\{F\}$  relationship in Blender involves:

- (a) Traversing all vertices (outer loop); for each vertex traverse the list of faces (inner loop)
- (b) Traversing all faces (outer loop); for each face traverse its vertices (inner loop)
- (c) Traversing all vertices (outer loop); for each vertex find its references in the list of faces
- (d) Traversing all faces first (one loop) and after that traverse all vertices (second loop)

**Question 12.** Given the quantities  $F, E, V$  of a valid polyhedron, how can we compute the number of half-edges?

**Question 13.** One algorithm for creating BRep approximations of a sphere consists in applying a 1:4 subdivision to an initial triangular mesh approximating a sphere (e.g. an octahedron). Assuming the initial solid has  $F$  faces,  $E$  edges and  $V$  vertices, indicate the resulting number of faces  $F'$ , edges  $E'$  and vertices  $V'$  after one step of 1-to-4 subdivision of its triangles.

**Question 14.** Given a polygon in 3D space, we know the areas ( $S_x, S_y, S_z$ ) of its projections onto the  $X=0, Y=0$  and  $Z=0$  planes. How can we compute the area of the polygon from these data?

**Question 15.** The output of a Catmull-Clark subdivision step produces

- (a) Faces with 3 or 4 vertices
- (b) Only triangles
- (c) Only quads
- (d) Faces with arbitrary number of vertices

**Question 16.** Concerning subdivision surfaces (answer YES/NO)

- (a) Is the Catmull-Clark surface guaranteed to go through the vertices of the input mesh?
- (b) Does the Doo-Sabin surface interpolate the centroid of the input faces?

**Question 17.** The following list contains all the vertices forming face 1. Sort the vertices to form a face (starting from V3), following the domino algorithm.

V 3: xyz, {4,1,6}, fromAoutB  
V 4: xyz, {2,1,6}, fromAoutB  
V 7: xyz, {4,1,12}, fromAoutB  
V 8: xyz, {5,1,2}, fromAoutB  
V20: xyz, {8,1,5}, New  
V22: xyz, {8,1,12}, New

V3,V4, ...

**Question 18.** Regarding the marching cubes algorithm, draw an example of ambiguous face and an example of non-ambiguous face.

**Question 19.** Given two solids A, B, indicate which vertices will be part of the Boolean difference A-B.

**Question 20.** Write a Python function for Blender that, given a Mesh object **with a single shell**, and its genus H, prints "OK" if and only if the mesh satisfies the Euler equation.

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def EulerCheck(mesh, H):
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